
Security Analysis of Distance Bounding Protocols

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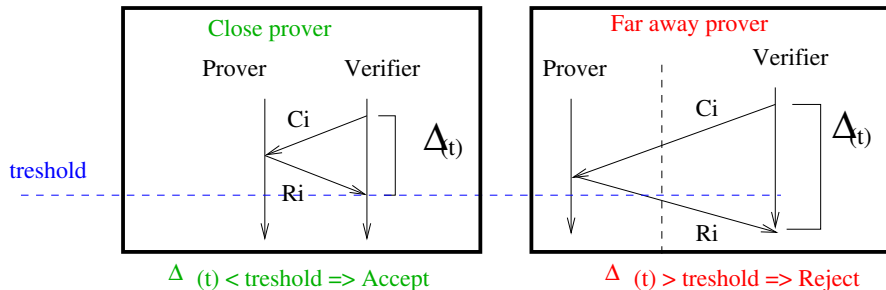
September 17th 2015





Relay Attacks on Passive Keyless Entry and Start Systems in Modern Cars,
A. Francillon, 2011

Counter measure : RTT check





Verifier V
public key : y

Prover P
secret key : x



Initialisation phase

← commit(m)

$m \xleftarrow{\$} \{0,1\}^n$

Distance Bounding phase

for $i = 1$ to n

Pick $c_i \in \{0,1\}$

Start clock

→ c_i

Stop clock

← r_i

$r_i := m_i \oplus c_i$

Check timers Δt_i

Verification phase

open commitment

Check responses

←

Check signature

← Sign $_x(S)$

$S := c_1 || r_1 || \dots || c_n || r_n$

→ Out $_V$

Distance Bounding Protocol



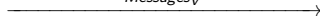
Verifier V
shared key : x

Prover P
shared key : x

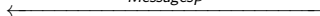


Initialisation phase

$Messages_V$



$Messages_P$



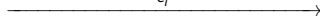
$$a = f_x(Messages_V, Messages_P)$$

Distance Bounding phase

for $i = 1$ to n

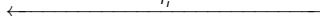
c_i

Start clock



r_i

Stop clock

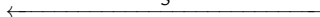


$$r_i = F(c_i, a_i, x_i)$$

Verification phase


S

Check Δt_i , r_i and S



$$S = \text{sign}_x(\text{transcript})$$

Mafia Fraud (MF) : an adversary \mathcal{A} tries to prove that a prover P is close to a verifier V .


$$\underbrace{P \leftrightarrow \mathcal{A} \leftrightarrow V}_{\text{far away}}$$

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Impersonation Fraud (IF) : an adversary tries to impersonate the prover to the verifier.

$$\mathcal{A} \leftrightarrow V$$





Distance Fraud : a far-away prover P^* tries to prove that he is close to a verifier V .

$$P^* \leftrightarrow V$$

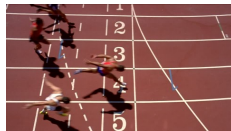


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$$P^* \leftrightarrow V$$

Distance Hijacking (DH) : a far-away prover P^* tries to prove that he is close to a verifier V by taking advantage of others provers P_1, \dots, P_n .

$$P^* \leftrightarrow P_1, \dots, P_n \leftrightarrow V$$



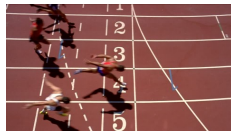


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Terrorist Fraud (TF) : a far-away prover P^* helps an adversary \mathcal{A} to prove that P^* is close to a verifier V without giving \mathcal{A} another advantage.

$$P^* \leftrightarrow \mathcal{A} \leftrightarrow V$$

- No exhaustive list of DB protocols.
- No compared or classified.
- No relationship between threat models.

- 1 Relations between Model of Threat
- 2 Attack and defence strategies
- 3 Conclusion and Perspective

1 Relations between Model of Threat

2 Attack and defence strategies

3 Conclusion and Perspective

Distance Fraud (DF) :

$$P^*(x) \leftrightarrow (P_1(x'), \dots, P'_m(x') \leftrightarrow V_1(y'), \dots, V_m(y') \leftrightarrow) V(y; r_V)$$

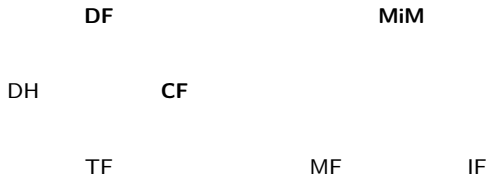
Man-In-the-Middle (MiM) :

$$P_1(x), \dots, P_m(x) \leftrightarrow \mathcal{A}_1 \leftrightarrow V_1(y), \dots, V_z(y) \\ P_{m+1}(x), \dots, P_l(x) \leftrightarrow \mathcal{A}_2(\text{View}_{\mathcal{A}_1}) \leftrightarrow V(y)$$

Collusion Fraud (CF) :

$$P^*(x) \leftrightarrow \mathcal{A}^{\text{CF}} \leftrightarrow V_0(y)$$

- $X \rightarrow Y$ denotes that if the property X is satisfied then Y is also satisfied, an attack on the property Y implies an attack on the property X .



The BMV Model(2013)



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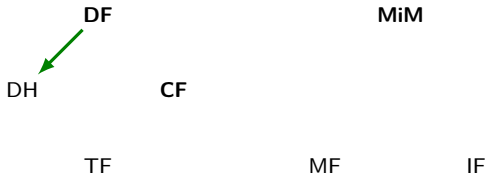
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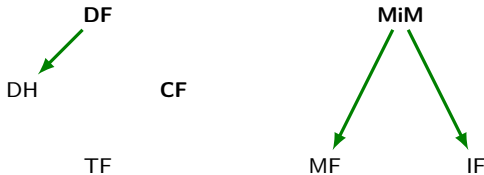
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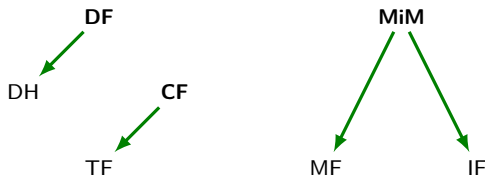
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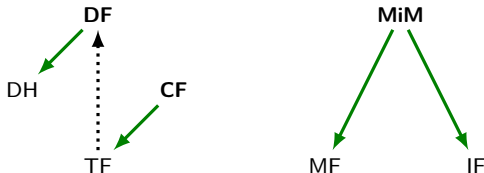
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- $X \dashrightarrow Y$ denotes that an attack on the property Y without sending the secret x implies an attack on the property X .

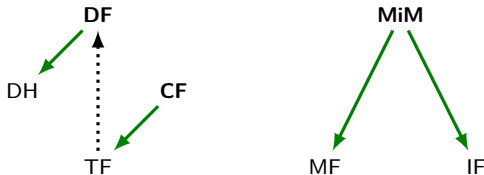


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Theorem (TF \dashrightarrow DF)

If a protocol is not α -resistant to DF, then there exists an attack of kind TF which succeed with probability at least α .

Proof : If $P^* \longleftrightarrow V$ succeeds, then $P^* \longleftrightarrow \mathcal{A}^{TF} \longleftrightarrow V$ succeeds with the same probability, if P^* does not transmit his secret and \mathcal{A}^{TF} simply relays messages. □

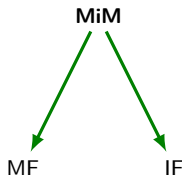
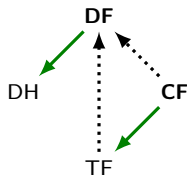


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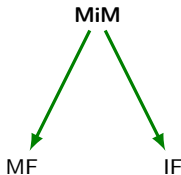
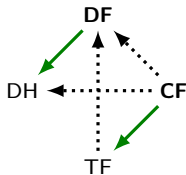


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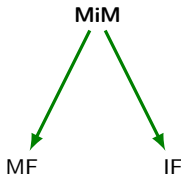
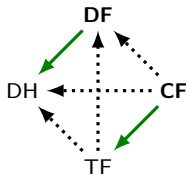


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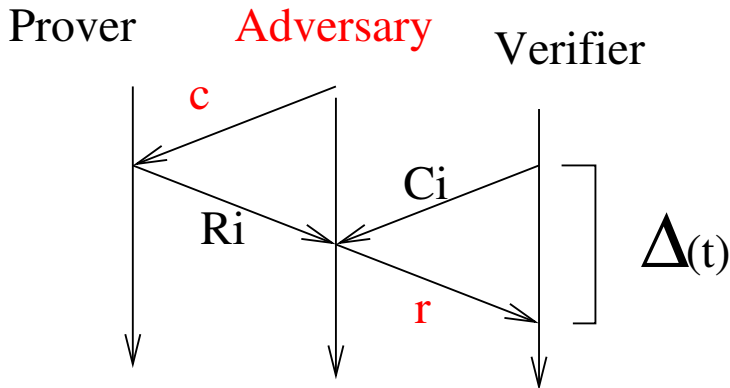


1 Relations between Model of Threat

2 **Attack and defence strategies**

3 Conclusion and Perspective

- Pre ask strategy



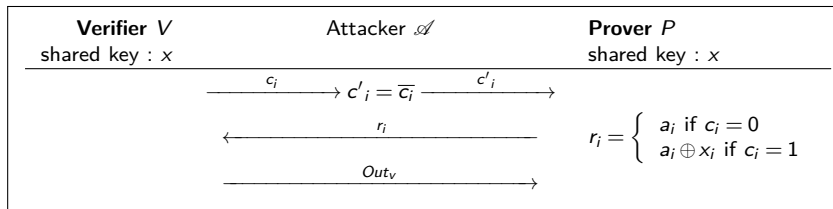
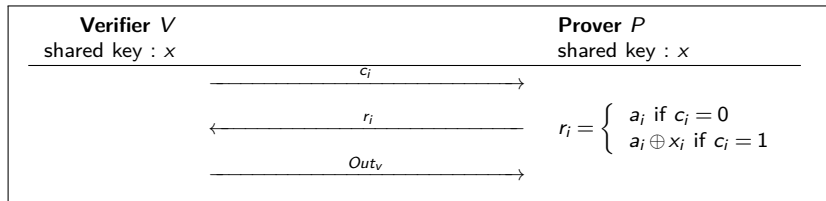
If $c == c_i$, \mathcal{A} knows r_i . Else, he has to guess. \mathcal{A} wins if he gives a good r_i at all rounds

$(\frac{1}{2} \cdot 1 + \frac{1}{2} \cdot \frac{1}{2})^n = (\frac{3}{4})^n$. Defence : Signature of the transcript

Attack Strategies : Impersonation Fraud

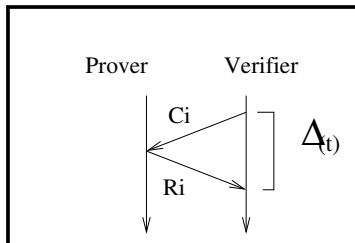


- Key recovery

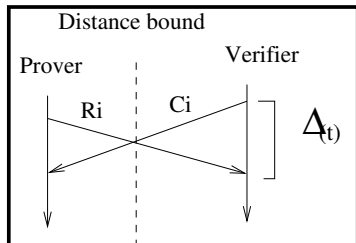


If $Out_v = 1$, $a_i = a_i \oplus x_i$, so $x_i = 0$. Else, $x_i = 1$. After n executions, \mathcal{A} recovers the whole key! **Defense** : The responses can not just be a xor between the key and a one time pad.

Normal scenario



Distance Fraud



Two possible responses : if $c_i = 0$, $r_i = a_i$ and if $c_i = 1$, $r_i = b_i$.
 $\left(\frac{1}{2} \cdot 1 + \frac{1}{2} \cdot \frac{1}{2}\right)^n = \left(\frac{3}{4}\right)^n$.

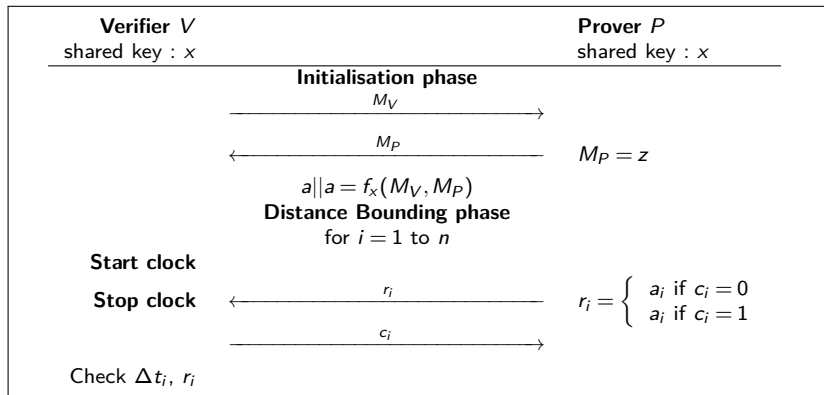
- Defence : The 2 possible responses should be complementary

Attack Strategies : Distance fraud : Example



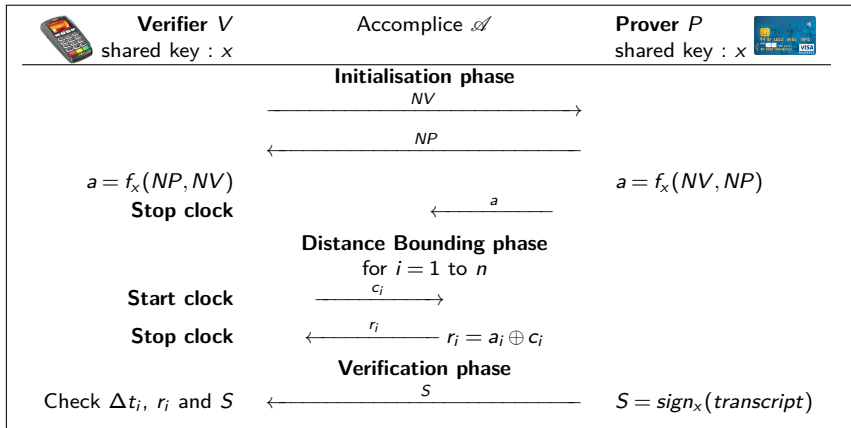
Let g be a PRF and f a PRF constructed as follows :

$$f_x(M_V, M_P) = \begin{cases} a||a & \text{if } M_P = z \\ g_x(M_V, M_P) & \text{otherwise} \end{cases} \quad f_x \text{ is a PRF.}$$



Defense : The PRF output should not be split in several parts.

Attack Strategies : Terrorist fraud



P can give a to \mathcal{A} and allow a terrorist fraud with success probability 1, since a does not link any information about the secret key. **Defense : Making the responses related to the key**

IF : Threat model few considered.
Exhaustive research on the key.
 $\left(\frac{1}{2}\right)^s$, where s is the size of the key.

DH : Threat model few considered.
 P^* hopes that P responds correctly to V .
 $\left(\frac{1}{2}\right)^n$, where n is the number of round in the DB phase.

TF : P^* gives responses to \mathcal{A} . So, TF mainly filled with 1.

- 82 improvements = 28 DH + 10 DF + 0 MF + 30 IF + 1 MiM + 13 TF/CF.

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- 9 survivors : no attacks with probability of success at 1.

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Protocols	Success Probability						
	DH	DF	MF	IF	MiM	TF	CF
KZP (2008)	$(\frac{1}{2})^n$	$(\frac{3}{4})^n$ [8]	$(\frac{1}{2})^n$ [8]	$(\frac{1}{2})^s$	$(\frac{1}{2})^n$ [8]	$(\frac{3}{4})^v$ [8]	$(\frac{3}{4})^v$ [8]
Hitomi (2010)	$(\frac{1}{2})^n$ [5]	$(\frac{3}{4})^n$	$(\frac{1}{2})^n$ [9]	$(\frac{1}{2})^n$	$(\frac{1}{2})^n$ [9]	$(\frac{3}{4})^v$ [9]	$(\frac{3}{4})^v$ [9]
NUS (2011)	$(\frac{1}{2})^n$	$(\frac{3}{4})^n$ [1]	$(\frac{1}{2})^n$ [7]	$(\frac{1}{2})^n$ [7]	$(\frac{1}{2})^n$ [7]	$(\frac{3}{4})^v$	$(\frac{3}{4})^v$
SKI _{pro} (2013)	$(\frac{1}{2})^n$	$(\frac{3}{4})^n$ [2]	$(\frac{2}{3})^n$ [2]	$(\frac{1}{2})^s$	$(\frac{2}{3})^n$ [2]	$(\frac{5}{6})^v$ [3]	$(\frac{5}{6})^v$ [3]
Fischlin & Onete (2013)	$(\frac{1}{2})^n$	$(\frac{3}{4})^n$ [10]	$(\frac{3}{4})^n$ [10]	$(\frac{1}{2})^{2s}$	$(\frac{3}{4})^n$ [10]	$(\frac{3}{4})^v$ [10]	$(\frac{3}{4})^v$ [10]
DB1 (2014)	$(\frac{1}{t})^n$	$(\frac{1}{t})^n$ [4]	$(\frac{1}{t})^n$ [4]	$(\frac{1}{2})^s$	$(\frac{1}{t})^n$ [4]	$(\frac{t-1}{t})^v$ [4]	$(\frac{t-1}{t})^v$ [4]
DB2 (2014)	$(\frac{1}{2})^n$	$(\frac{1}{\sqrt{2}})^n$ [4]	$(\frac{1}{2})^n$ [4]	$(\frac{1}{2})^s$	$(\frac{1}{2})^n$ [4]	$(\frac{1}{\sqrt{2}})^v$ [4]	$(\frac{1}{\sqrt{2}})^v$ [4]
ProProx (2014)	$(\frac{1}{2})^{n-s}$	$(\frac{1}{\sqrt{2}})^{ns}$ [11]	$(\frac{1}{2})^{ns}$ [11]	$(\frac{1}{2})^s$ [11]	$(\frac{1}{2})^{ns}$ [11]	$(\frac{1}{\sqrt{2}})^{ns}$ [11]	$(\frac{1}{\sqrt{2}})^{ns}$ [11]
VSSDB (2014)	$(\frac{1}{2})^n$	$(\frac{3}{4})^n$ [6]	$(\frac{1}{2})^n$ [6]	$(\frac{1}{2})^{2s}$ [6]	$(\frac{1}{2})^n$ [6]	$(\frac{3}{4})^v$ [6]	$(\frac{3}{4})^v$ [6]

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2 Attack and defence strategies

3 Conclusion and Perspective

- The **relationship** between threats models.
- Identify more easily the properties of a DB protocols.
- Compilation and classification of **42 protocols**.
- **Graph of dependency**.
- **82 improvements** of attacks.
- **9 still secure** protocols.
- **Tool box** : strategies of attack/defense.

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Futur works :

- Formal verification.
- Best protocol design.

Thanks for your attention !

Questions ?

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